Inelastic relaxation and noise temperature in S/N/S junctions

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Abstract. We studied electronic relaxation in long diffusive superconductor/normal metal/superconductor (S/N/S) junctions by means of current noise and transport measurements down to very low temperature (100 mK). Samples with normal metal lengths of 4, 10 and 60 μ m have been investigated. In all samples the shot noise increases very rapidly with the voltage. This is interpreted in terms of enhanced heating of the electron gas confined between the two S/N interfaces. Experimental results are analyzed quantitatively taking into account electron-phonon interaction and heat transfer through the S/N interfaces. Transport measurements reveal that in all samples the two S/N interfaces are connected incoherently, as shown by the reentrance of the resistance at low temperature. The complementarity of noise and transport measurements allows us to show that the energy dependence of the reentrance at low voltage is essentially due to the increasing effective temperature of the quasiparticles in the normal metal.

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The profound comprehension of the current transport in metals is a topic of permanent interest [1,2]. With the progress in thin film technology a great number of studies deal with coherence phenomena at low temperature in metallic samples of length L shorter than the phase coherence length L_{ϕ} (mesoscopic regime). In this context, a lot of works focus on inelastic processes and for instance, on the apparent saturation of the phase breaking length [3,4]. Current noise measurement is particularly well suited to such investigations because it is sensitive to energy relaxation processes and gives access to the involved inelastic scattering length L_{in} [5,6].

Current noise in diffusive mesoscopic normal metals connected to two normal reservoirs (N/N/N-case) has been studied by various groups [7–9]. Using a Boltzmann-Langevin approach the current noise is given by [10]:

$$S_I = \frac{4}{RL} \int_{-L/2}^{L/2} \mathrm{d}x \int \mathrm{d}\epsilon \, f(\epsilon, x) [1 - f(\epsilon, x)], \qquad (1)$$

where f is the distribution function of the electrons and Rthe resistance of the sample. In the regime $L \ll L_{in}$, the noise is reduced by a factor 3 compared to the Schottky value 2eI. If the length of the sample exceeds L_{in} , the electron gas can be described by a Fermi distribution with an effective temperature T_e and equation (1) simplifies to:

$$S_I = \frac{4k_B}{RL} \int_{-L/2}^{L/2} \mathrm{d}x \, T_e(x) = \frac{4k_B \overline{T_e}}{R} \,. \tag{2}$$

Electron-electron (e-e) and electron-phonon (e-ph) scattering affect the noise differently. On one hand, the e-e interaction redistributes the energy of the electron system and T_e increases due to an increasing number of electronic states that contribute to the noise. On the other hand, the power injected by the bias current in the sample can be dissipated to the lattice through e-ph interaction and T_e decreases.

In S/N/S junctions, coherent electron-hole pairs penetrate from the superconductor into the normal metal over a distance $L_c = \min(L_{\phi}, \xi_{\epsilon} = \sqrt{\hbar D/\epsilon})$ with $\epsilon = \max(k_B T, eV)$ and D the diffusion constant of the normal metal. If the sample length is smaller than L_c (coherent case), the phase coherence covers the entire normal region and the Josephson effects determine conductance and noise behavior at low voltage. In this case, the conductance exhibits clear subgap structures (SGS) and the noise is strongly enhanced compared to the normal case due to the coherent transfer of large charge quanta [11,12].

In this paper we consider the incoherent case where $L \gg L_c$. This regime has been recently studied theoretically by Bezuglyi *et al.* [13] and Nagaev [14]. They show that the noise is enhanced compared to normal junctions (N/N/N) because of the confinement of the subgap

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electrons in the normal part between the superconducting electrodes. If no inelastic processes take place ("collisionless regime") and in the zero temperature limit the noise increases linearly with the bias voltage:

$$S_I(V) = \frac{2}{3R}(eV + 2\Delta), \tag{3}$$

where Δ is the gap of the superconductor.

A simplified model to illustrate this behavior is the following: an electron with an energy $eV \ll \Delta$ can not escape in the superconducting reservoirs due to the absence of electronic states in the gap. Instead, it enters the superconductor together with a second electron as a Cooper pair and a hole is retroreflected in the normal metal (Andreev reflection). The reflected hole travels the normal region a second time and is retroreflected as an electron at the other S/N interface and so on. In the incoherent case the phase information between two subsequent Andreev reflections is lost. Therefore the quasiparticles experience Incoherent Multiple Andreev Reflections (IMAR). During each travel across the junction, the gain in energy is equal to eV, where V is the applied voltage. Therefore the quasiparticles travel the normal part of the junction N times with $N = int[2\Delta/(eV) + 1]$ before acquiring enough energy to escape in the superconducting electrode. Within this description, the total noise is the shot noise in a diffusive normal metal at zero temperature $\frac{1}{3}2eI$ times N.

At low voltage and finite temperature, the effective length of the junction for the multiply retroreflected particles $L_{eff} = NL \sim L\Delta/V$ exceeds the inelastic length L_{in} . In this "interacting regime" e-e-collisions interrupt the IMAR cycle before the quasiparticles reach the gap. In the case of strong interaction a Fermi distribution with an effective temperature T_e is restored. T_e decreases with decreasing voltage and reaches equilibrium (lattice temperature) at zero bias. Simultaneously the noise drops from the strongly enhanced level described by equation (3) to the Johnson-Nyquist level. Contrary to the N/N/N-case, e-e-interactions reduce the energy window of the involved electronic states.

Note that the voltage dependence of the effective length L_{eff} in S/N/S junctions provides a unique way to study inelastic interactions in a normal metal because the same sample can be tuned from the strongly thermalized regime to the collisionless regime simply by changing the applied voltage.

On the experimental side only a few results are reported on current noise in incoherent diffusive S/N/S junctions at present. Besides measurements on short (coherent) junctions, Hoss *et al.* [12] also addressed the incoherent case. They studied 2 μ m long Nb/Au/Nb junctions in the interacting regime over the entire voltage range because of the large superconducting gap of Nb. In a paper by Roche *et al.* [17] the length of the normal part is also about 2 μ m, and despite the use of a high mobility 2DEG as the normal part, the e-ph scattering rate is high enough to drive the junction in the interacting regime. Finally Jehl *et al.* studied Nb/Al/Nb junctions at relatively high temperatures which behave as two S/N contacts in series [15].



Fig. 1. Photography of a typical sample (here $L = 4 \ \mu m$) and schematic cross section. All the dimensions scale with the length L.

Using a different technique Pierre *et al.* measured directly the distribution function in long S/N/S junction but only at energies above the gap [16].

Whereas all these works investigated contacts with a length $L \leq 5 \ \mu$ m, we deliberately choose to study longer junctions (4, 10 and 60 μ m) to determine the respective role of e-e collisions, e-ph collisions and heat transfer through the S/N interfaces on the shot noise in S/N/S junctions. Moreover, to see the crossover from the interacting regime to the collisionless regime, we used aluminium because of its small superconducting gap. Because of the very small phase coherence length in the normal metal we used (see below), we have an almost perfect realization of the regime of IMAR.

To measure the current fluctuations we used a SQUIDbased experimental setup [18]. The intrinsic noise is about $10 \mu \Phi_0 / \sqrt{Hz}$ which is equivalent to $2 pA / \sqrt{Hz}$ in the input coil of the SQUID. The same experimental setup has been used to perform transport measurements.

Samples were fabricated by DC magnetron sputtering and optical lithography. First, a bilayer of Al/Cu (130 nm/30 nm) is deposited in situ to ensure a good contact between the two metals. This bilayer is etched to define the electrodes. Then the copper bridge (thickness 130 nm, purity of the Cu target: 99.9999%) is deposited by lift-off, preceded by a short backsputtering to clean the copper surface. Finally the whole sample is etched to remove the copper film from the aluminium electrodes. The resulting thickness of the copper bridge is 90 nm. A typical sample and a schematic cross section are shown in Figure 1.

We studied junctions with 3 different lengths L: 4, 10 and 60 μ m, but with the same width/length ratio: $w/L \approx 3/2$. All samples originate from the same wafer. In spite of very different overlap surfaces between aluminium and copper (because all dimensions scale with the length L), all samples have roughly the same resistance of about 0.65 Ω , which indicates a good interface (small barrier resistance). Below the transition of the Al electrodes at 1.5 K and the transition of the Al/Cu bilayer (overlap region) at about 1 K (see right inset of Fig. 2), the measured resistance is therefore essentially that of the normal part



Fig. 2. Differential resistance dV/dI versus DC voltage at 100 mK for 3 samples with different lengths (data for the 60 μ m sample are shifted by +0.06 Ω). Right inset: Resistance versus temperature for a slightly different 4 μ m sample. Left inset: The resistance of the 3 samples at very low temperatures.

of the junctions. We then deduce the diffusion constant in copper: $D = 30 \text{ cm}^2 \text{ s}^{-1}$. We confirmed this value by measuring the resistance of a meander line consisting of 700 squares in series, which was cosputtered on the same wafer.

In the temperature range from 1 K to 0.3 K the resistance decreases as expected in the classical proximityeffect. This fact and the reduced transition temperature of the bilayer are other indications of clean S/N interfaces. The resistance does not go down to zero since the sample lengths are much greater than the thermal length $L_T = \sqrt{\frac{\hbar D}{k_B T}} \approx 0.9 \ \mu \text{m}$ at T = 30 mK. Therefore no supercurrent is observed. On the contrary, at low temperatures (T < 0.3 K), the resistance increases again. This behavior is very similar to the reentrance in S/N junctions first observed by Charlat *et al.* [19]. It means the two S/N interfaces of the junctions are connected incoherently. The temperature T_r at which the resistance behavior changes is related to the phase breaking length L_{ϕ} by $k_B T_r \approx \hbar D / L_{\phi}^2$ [22] (leading to $L_{\phi} \approx 0.3 \ \mu \text{m}$) and is independent of L (see left inset of Fig. 2). Such a large phase breaking rate is usual for Cu layers probably because of paramagnetic centers in the Cu oxide at the surface [20,21]. The relative amplitude of the reentrance increases as the length L decreases since the relative volume of the sample which is affected by coherent pairs increases.

The voltage dependence of the differential resistance dV/dI measured at T = 100 mK (Fig. 2) confirms the reentrance behavior. As for the temperature dependence, the amplitude and width of the reentrance peak depend on the width of the sample. However, we clearly see that the voltage needed to destroy the effect (2 μ V and 4 μ V for the 4 μ m and 10 μ m samples) is much smaller than $\frac{k_B}{e}T_r$. As suggested in other experiments [22,23], this apparent discrepancy is due to a heating effect. Because we performed conductance and noise measurements simultaneously, we



Fig. 3. Current noise density times the resistance R = V/Iversus DC voltage at T = 100 mK. Dot-dashed line: expected noise of 2 S/N junctions in series. Solid straight line: Theoretical prediction [13,14] in the collisionless regime with $\Delta = 135 \ \mu eV$. Dashed line: Fit taking into consideration e-ph interaction (see text).

know the electronic temperature at low voltage. Anticipating the detailed description of noise measurements below, we found that the electron gas reaches a temperature of 0.23 K at 2 μ V for the 4 μ m sample and 0.2 K at 4 μ V for the 10 μ m sample. Consequently the rapid destruction of the reentrance peak is essentially due to the dramatic increase of T_e at low bias voltage.

At higher voltage ($V \approx 70 \ \mu V$) the bilayer (or at least part of it) is driven in the normal state, and a large peak occurs in the differential resistance (not shown). dV/dI changes by only approximately 10% up to $V = 70 \ \mu V$ and over this voltage range, we do not observe subharmonic gap structures (SGS) as expected in our experimental situation.

SGS appear at voltages $V = 2\Delta/ne$ due to the singularity in the DOS of the superconductor at the gap edges and, especially for junctions with high transparent interfaces, to the strongly enhanced probability of Andreev reflection at low energy. The latter is caused by the proximity effect in the normal metal [24]. In our samples the DOS singularities are smeared by the bilayer structure of the electrodes (Al/Cu with good interface) and the proximity corrections are very small because of the very short correlation length L_c . Moreover the SGS of high order $(n \geq 4$ because 70 μ eV $\approx \Delta/2$) are usually very weak and additionally smeared out by inelastic scattering at low voltage.

The results of the noise measurements at T = 100 mK are shown in Figure 3 where we have plotted the current noise density S_I times the resistance R = V/Iversus DC voltage. The noise increases more rapidly with the bias voltage than what is expected for two independent S/N junctions in series with a reservoir in between (see dot-dashed line in Fig. 3), and we do not see the thermal crossover towards the Johnson-Nyquist noise level at $eV \approx k_B T \approx 9 \ \mu$ V. The noise enhancement in these S/N/S junctions is due to the confinement of the quasiparticles between the two superconducting electrodes. With increasing sample length the confinement is relaxed by eph interaction and the noise slope at low voltage becomes less important.

At $V \approx 50 \ \mu\text{V}$, the noise of the 4 μm sample approaches a straight line compatible with the prediction in the collisionless regime (Eq. (3)) with $\Delta = 135 \ \mu\text{eV}$. The gap value is reduced compared to the pure Al film ($\Delta \approx 200 \ \mu\text{eV}$) because of the bilayer structure of the superconducting electrodes. The reduction factor is the same as for the transition temperature.

At higher voltages ($V \ge 70 \ \mu V$) the noise shows an irregular behavior which reflects the transition of the bilayer. In this voltage range, all IMAR cycles end by injecting a quasiparticle above the gap in the superconductor. Consequently, many quasiparticles arrive in the superconducting electrodes and weaken the superconductivity. Therefore, the voltage driven transition of the bilayer could be related to the collisionless regime itself.

In the following we focus on the interacting regime at low voltage where the electron gas can be described by a Fermi distribution function with an effective temperature T_e . Unlike normal junctions where the injected power can be evacuated in the reservoirs, in S/N/S junctions only quasiparticles with energy above the gap can dissipate power. When the sample length is long enough, some heat can be transferred to the phonons through eph-scattering. These two mechanisms are covered with our experiments since we studied long to very long junctions.

For the longest junction (60 μ m) we suppose cooling by phonons to be dominant. The electron temperature T_e is then nearly constant over the whole sample length and can be calculated by a heat-diffusion equation [9,26]. It yields:

$$T_e = \left(\frac{P}{\Sigma\Omega} + T_{ph}^5\right)^{1/5},\tag{4}$$

where P is the power injected in the sample, Ω its volume and T_{ph} the temperature of the phonon bath (equal to the temperature of the mixing chamber). The parameter Σ is the e-ph coupling constant [26]. The noise is then given by $4k_BT_e/R$ and we obtain the best fit (see Figs. 3 and 4) for $\Sigma = 2.4 \times 10^9$ W m⁻³ K⁻⁵, a value which is of the same order of magnitude as reported for Au, Ag, Cu and AuCu [9,16,25,26].

For the shortest junctions (4 μ m) e-ph-scattering is not very efficient because the volume Ω is much smaller and the main cooling mechanism is the heat transfer by quasiparticles through the S/N interfaces outside the gap region. Following Bezuglyi *et al.* [13] the noise at low voltage is given by the Nyquist formula with a cut off at T_e of the order of Δ :

$$S_I = \frac{4k_B T_e}{R} \left(1 - 2 \exp\left[-\frac{\Delta}{k_B T_e}\right] \right) \cdot$$
(5)

Here the reservoirs are supposed at T = 0 K. In fact, we can neglect the finite temperature of the electrodes



Fig. 4. Total power injected in the junctions as a function of the effective electron temperature in the normal part at a base temperature T = 100 mK (symbols) and theoretical predictions: thin solid lines – power dissipated by e-ph-scattering according to equation (4) for the 3 samples respectively; thick solid line – power dissipated through the S/N interfaces according to equation (6) for the 4 μ m sample; dashed line – sum of the contributions of the two cooling mechanisms for the 10 μ m sample.

because the quasiparticle temperature is rapidly much larger than the base temperature. From the measured noise $S_I(V)$ we obtain the effective electron temperature in the normal metal as a function of voltage $T_e(V)$ solving equation (5) numerically with $\Delta = 135 \ \mu eV$.

Figure 4 shows the total power V^2/R as a function of the effective temperature of the quasiparticles. For the 4 μ m sample, we then compare the experimental results to the theoretical prediction obtained by Bezuglyi *et al.* [13] who derived the power dissipated through the S/N interfaces as a function of the effective electron temperature at small voltage $eV \ll \Delta$ in good agreement with numerical simulations by Nagaev [14]. The fit in Figure 4 (thick solid line) is given by:

$$P_{NS} \approx \frac{V^2}{R} = \frac{k_B T_e \Delta}{e^2 W_{\epsilon} R} \left(1 + \frac{k_B T_e}{\Delta} \right) \exp\left[-\frac{\Delta}{k_B T_e} \right] \cdot \quad (6)$$

with $W_{\epsilon} = \tau_{ee}(\Delta)/\tau_D$ where $\tau_{ee}(\Delta)$ is the e-e-scattering time at the gap energy and τ_D the diffusion time. We obtain good agreement between the experimental data and the prediction with $W_{\epsilon} = 0.7 \pm 0.2$. This value is of the same order as the theoretical estimation of W_{ϵ} ($W_{\epsilon} = 2.3$) using the standard theory of e-e-interaction in a 2D geometry [28]. A small but finite interface resistance would renormalize this estimation [24] and could give a better agreement. The fact that $W_{\epsilon} \approx 1$ indicates that the e-escattering time at the gap energy is of the order of the diffusion time $\tau_D \approx 5$ ns and is two orders of magnitude larger than the phase coherence time found above ($L_{\phi} \approx 0.3 \ \mu m$ corresponds to $\tau_{\phi} \approx 0.03$ ns).

Note that the theoretical model applied here is especially dedicated to incoherent S/N/S junctions and

therefore more appropriate than the usually used Blonder-Tinkham-Klapwijk (BTK) model [12,27,29] and its derivatives [30].

For comparison we also plotted in Figure 4 the power P_{ph} dissipated by the phonons in the 4 μ m sample using the value of Σ obtained for the 60 μ m sample (thin solid line). In the range 200 to 600 mK, P_{ph} is about five times smaller than P_{NS} and the error that we make neglecting this contribution is covered by the uncertainty on W_{ϵ} given above.

Concerning the intermediate sample of length 10 μ m the power dissipated by phonons and through the interfaces is of the same order of magnitude. Extracting T_e from equation (5), we fit the total power by adding the contributions of the two cooling mechanisms, treated separately according to equations (4, 6). We obtain good agreement (see dashed line in Fig. 4) with the following parameters: $\Delta = 135 \ \mu$ eV, the same value of Σ as for the 60 μ m sample and $W_{\epsilon} = 0.3 \pm 0.1$ (theoretical estimation $W_{\epsilon} \approx 0.4$).

In conclusion, we investigated IMAR enhanced current noise in long S/N/S junctions of very different lengths $(4, 10 \text{ and } 60 \ \mu\text{m})$. We found that the noise temperature increases very rapidly at low voltage. We deduce the energy dependence of the thermal conductivity of the S/N interfaces which is in good agreement with recent semiclassical theory [13,14]. The noise behavior of the longest sample can be well fitted taking into account only phonon cooling. The inelastic scattering times we deduced are in agreement with standard description of e-e and e-ph interaction. With the same experimental setup we performed transport measurements. They reveal that in all the samples the two S/N interfaces are connected incoherently, indicating $L_{\phi} \ll L_{in}$. The complementarity of transport and noise measurements provided a direct analysis of the voltage dependence of the reentrance in terms of an effective electron temperature.

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